

*Metro MEGT, October 2016*

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# Ten Plus One:

Enhancing Depth and Complexity of Math Tasks

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$$35 - 18$$

$$3\frac{1}{3} - 1\frac{5}{6}$$

Simplify  $\frac{18}{21}$

Name the shape.



$$12 \times 10$$

Find the mean and median: 31, 27, 32, 65, 29

$$35\% \text{ of } 120$$



Measure the angle

Seventy-four is \_\_\_\_ tens and \_\_\_\_ ones



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# Goals

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- ❖ *Learn* strategies for creating deep math tasks.
- ❖ *Apply* strategies for creating deep math tasks.
- ❖ *Anticipate* students' thinking.
- ❖ *Envision* classroom implementation.
- ❖ *Discuss* additional resources.

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# Mathematical Depth

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## Less depth

What do I *do*?

What are the *steps*?

How can I *remember*?

## More Depth

What do I *think*?

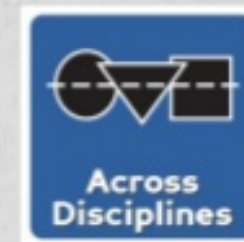
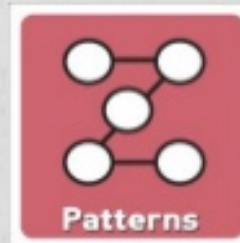
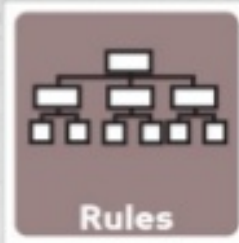
What does it *mean*?

How does it *connect*?



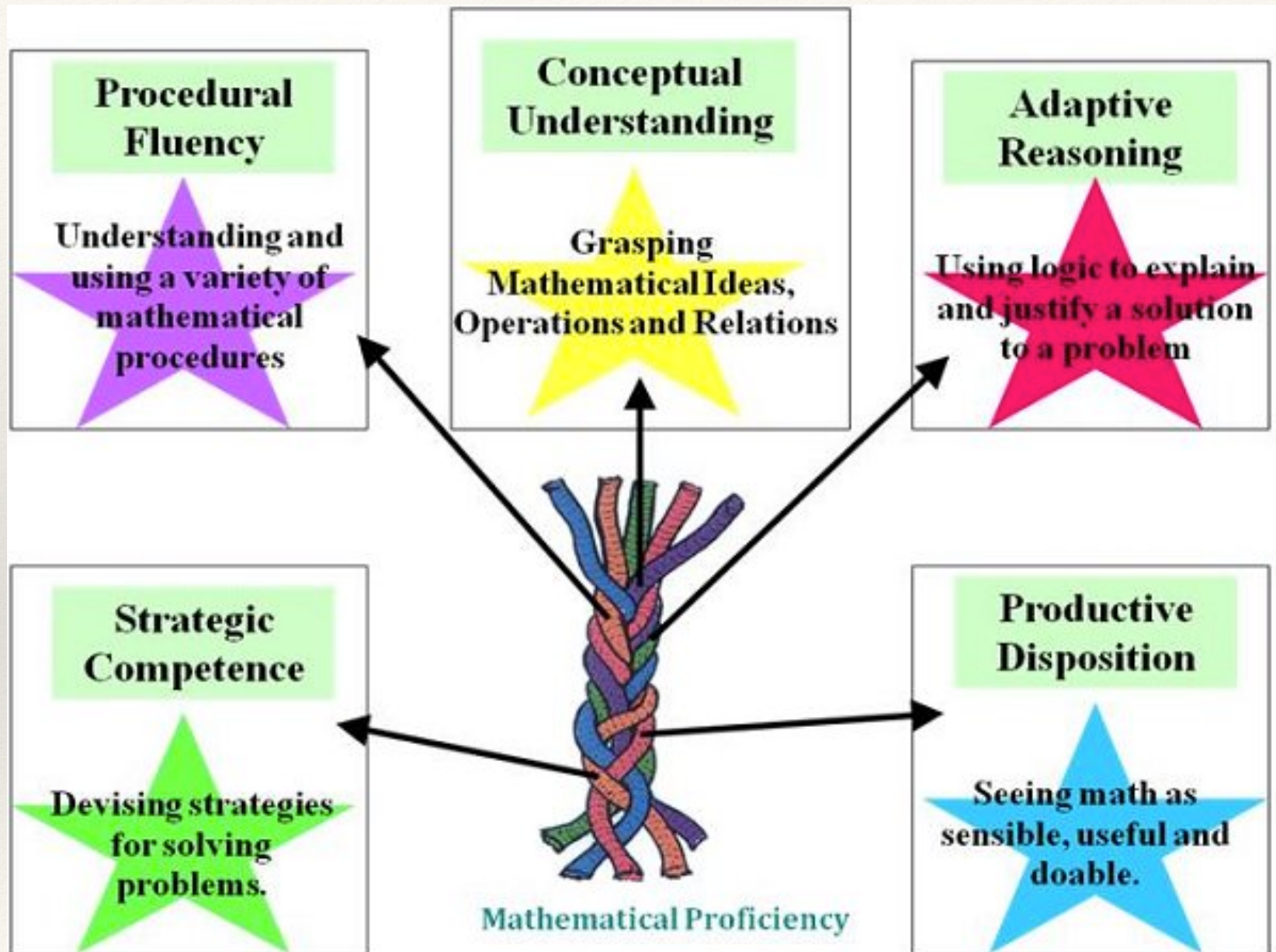
# Kaplan's Icons

## DEPTH & COMPLEXITY ICONS



Based upon the work of Sandra Kaplan, USC

# Math Proficiency Strands



Kilpatrick, J., Swafford, J., Findell, B. (Ed.). (2001). Adding it up: helping children learn mathematics. Washington, DC: National Academy Press.



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# NCTM Process Standards

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- ❖ Problem Solving
  - ❖ Develop, apply, and verify your own strategies to answer questions.
- ❖ Reasoning and Proof
  - ❖ Make and test predictions. Analyze and extend patterns. Justify conclusions.
- ❖ Communication
  - ❖ Organize, record, and present mathematical ideas clearly (orally and in writing).
- ❖ Connections
  - ❖ Recognize relationships among mathematical ideas and between math and other disciplines.
- ❖ Representations
  - ❖ Model math concepts with words, graphs, tables, symbols, pictures, manipulatives, etc.

adapted from *Principles and Standards for School Mathematics*. Reston, Va.: NCTM, 2000.



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# Connecting Kaplan to Best Practices in Math

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Conceptual Understanding	<b>Big Idea</b> , Patterns, Trends, Different Perspectives
Procedural Fluency	<b>Rules</b> , Ethics, Different Perspectives
Adaptive Reasoning	<b>Patterns</b> and <b>Details</b> , Trends, Different Perspectives
Strategic Competence	<b>Unanswered Questions</b> , Different Perspectives, Ethics
Mathematical Communication	<b>Language of the Discipline</b> , Rules, Different Perspectives
Connections	<b>Across the Disciplines</b> , Different Perspectives, Patterns
Representations	<b>Different Perspectives</b> , Language of the Discipline



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# The Ten Plus One Process

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1. **Identify** a math task.
2. **Choose** a *Ten Plus One* strategy.
3. **Apply** the strategy to enhance the task.
4. **Anticipate** students' thinking.

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# A Ten Plus One Template

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1. Identify a math task.	4. Anticipate students' thinking.
2. Choose a <i>Ten Plus One</i> strategy.	
3. Apply the strategy to enhance the task.	



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# Ten Strategies

## for Creating Deep Math Tasks

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1. Write a story.
2. Draw a picture.
3. Explain why.
4. Find another way.
5. Compare and contrast.
6. Start with the answer.
7. Remove information.
8. Solve to learn.
9. Build a pattern.
10. Ask “What if...?”

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# One Strategy

## for Creating Complex Math Tasks

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Use *more...*

digits, numbers, shapes, parts, variety, steps, ideas,  
information, definitions, categories, relationships, etc.

**Caution: The purpose is not just messy computation.**



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# Creating Tasks

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**Combine strategies.**

*Mix and match.*

**Skip strategies.**

*If a strategy doesn't work, let it go.*

**Be flexible.**

*Let the strategies inspire **your** creativity!*

**Focus on concepts.**

*Build on ideas underlying the task.*

**Take the long view.**

*Improve your tasks over time.*



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# Using the Tasks

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**Step back.**

*Let your students do the thinking.*

**Allow collaboration.**

*Help students learn from each other.*

**Expect explanations.**

*Deep and complex ideas are worth expressing!*

**Learn as you go.**

*Refine tasks using your students' ideas!*

**Save work samples.**

*Use student work for exemplars and assessments.*



*Thank you!*



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